

## ROTATION DAY 3: TORQUE & LEVER ARM

**WARM-UP (3 min):** You need to loosen a stuck bolt. Rank these strategies by effectiveness (easiest to hardest):

- **A:** Push with 50 N using a long wrench, at the end, perpendicular to the wrench.
- **B:** Push with 100 N using a short wrench, at the end, perpendicular.
- **C:** Push with 100 N using a long wrench, but pushing at 30° to the wrench.
- **D:** Push with 100 N at the middle of the long wrench, perpendicular.

**Prediction:** \_\_\_ > \_\_\_ > \_\_\_ > \_\_\_ After we learn the equation, we'll check your ranking.

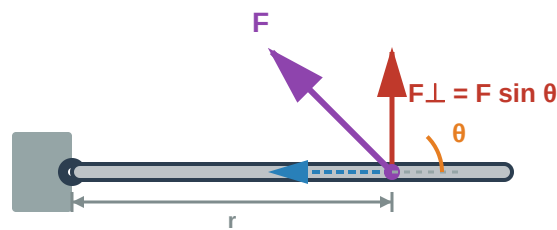
### WHAT MAKES THINGS ROTATE?

#### TORQUE

$$\tau = rF \sin \theta$$

#### Where:

- $r$  = distance from pivot to where force is applied (m)
- $F$  = magnitude of force (N)
- $\theta$  = angle between the position vector and force vector
- $\tau$  = torque (N·m — NOT joules!)



#### Two equivalent ways to think about it:

(1)  $\tau = (r \sin \theta) F = (\text{lever arm}) \times (\text{full force})$ , or

(2)  $\tau = r(F \sin \theta) = (\text{full distance}) \times (\text{perpendicular component of force})$ .

Both give the same answer.

#### WE DO Check the Warm-Up Rankings

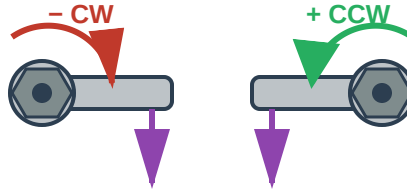
Now calculate  $\tau$  for each bolt scenario:

Strategy	$r$ (m)	$F$ (N)	$\theta$	$\tau = rF \sin \theta$ (N·m)
A	0.30	50	90°	
B	0.15	100	90°	
C	0.30	100	30°	
D	0.15	100	90°	

## SIGN CONVENTION FOR TORQUE

### POSITIVE AND NEGATIVE TORQUE

- **CCW = positive  $\tau$**  (like standard math angles)
- **CW = negative  $\tau$**



**Common mistake:** Students assign the sign based on the direction of the force (up = positive). Wrong! The sign depends on which WAY the force would make the object rotate around the pivot.

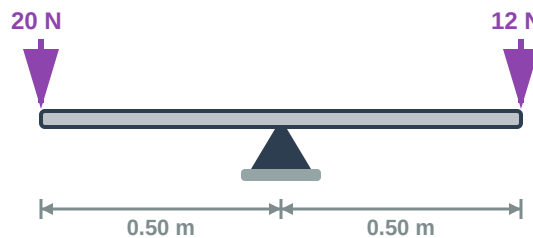
### Physics in the Wild: The Cheater Bar

When a mechanic can't break a bolt loose, they slide a long pipe over the wrench handle — called a "cheater bar." It doubles or triples  $r$  while  $F$  stays the same, so torque skyrockets. Some cheater bars are over a meter long. Medieval castle doors had long handles for exactly the same reason: more torque from a weaker push.

**Quick math:** If a mechanic applies 200 N with a 0.30 m wrench and can't break a bolt free, what happens when they add a 0.60 m pipe? How much torque now?

### WE DO Beam with Two Forces

A 1.0 m beam is pivoted at its center. A 20 N force pushes DOWN at the left end; a 12 N force pushes DOWN at the right end.



(a) Torque from left force (with sign):

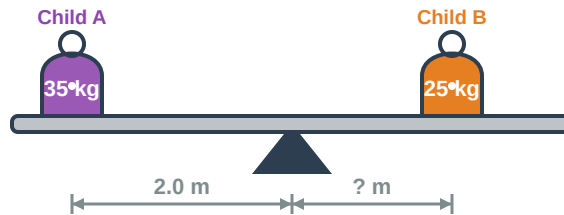
(b) Torque from right force (with sign):

(c) Net torque:

(d) Which way will the beam rotate?

**MULTIPLE TORQUES — NET TORQUE****WE DO** Playground Seesaw

Two children sit on a seesaw (pivot in middle). Child A (mass 35 kg) sits 2.0 m from the pivot. Child B (mass 25 kg) sits on the other side.

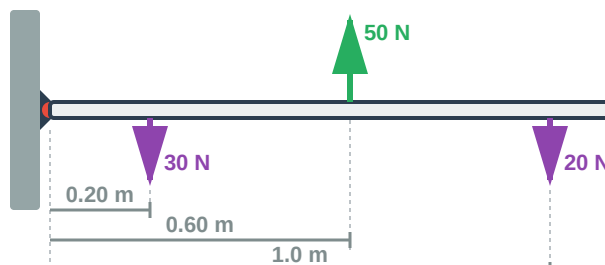


(a) Find the torque from Child A's weight about the pivot.

(b) How far from the pivot must Child B sit to balance the seesaw? (Set  $\Sigma\tau = 0$ .)

**YOU DO** Three Forces

A horizontal beam is pivoted at the left end. Forces: 30 N down at 0.20 m from pivot, 50 N up at 0.60 m from pivot, 20 N down at 1.0 m from pivot.



(a) Calculate each torque (with sign):

(b) Find net torque:

(c) Which way does the beam tend to rotate?

## EXIT TICKET & HOMEWORK

**EXIT TICKET:** A wrench is 0.25 m long. You apply 80 N at the end, perpendicular to the wrench.

(a) Find the torque:

(b) If you instead push at  $45^\circ$  to the wrench, what torque do you produce?

### HOMEWORK

#### PROBLEM 1 Conceptual — Revolving Door

A force is applied to a revolving door. In which case is the torque greatest?

- (a) Pushing at the outer edge, perpendicular.
- (b) Pushing at the outer edge, at  $45^\circ$ .
- (c) Pushing halfway to center, perpendicular.
- (d) Pushing at the outer edge, parallel to the door.

Circle answer: \_\_\_\_\_ Explain in one sentence:

#### PROBLEM 2 Lever Arm Practice

A mechanic uses a 0.40 m wrench and applies 120 N at  $75^\circ$  to the wrench. Calculate the torque.

#### PROBLEM 3 Two-Force Balance

A uniform meter stick (mass 0.15 kg) is supported at the 40 cm mark. A 0.50 kg mass hangs at the 10 cm mark. Where should a 0.30 kg mass be placed to balance the stick? (Remember: the stick's weight acts at its center of mass — the 50 cm mark.)

**Tomorrow: Static Equilibrium.** Two conditions:  $\Sigma F = 0$  AND  $\Sigma \tau = 0$ . It's Newton's Laws meets torque.