

# KINEMATICS DAY 10: PROJECTILES — ANGLED LAUNCH

## WARMUP Day 9 Review

A ball is launched horizontally from a fixed-height cliff. If its launch speed doubles, what happens?

- ☐ **A.** Fall time doubles; range stays the same      ☐ **B.** Fall time stays the same; range doubles  
☐ **C.** Both fall time and range double      ☐ **D.** Both fall time and range stay the same

Check one → convince your neighbor in one sentence.

**Physics in the Wild — Why Nobody Punts at 45°:** In a vacuum, 45° gives maximum range. Real punters kick closer to 50–55° — they're buying *hang time* so the coverage team can get downfield, trading distance for the bigger  $v_y$ . Once you can split a launch into components, trade-offs like that are one line of algebra.

## ANGLED LAUNCH = DAY 8 + DAY 9

**Step 1 — resolve:**  $v_{0x} = v_0 \cos \theta$  (stays constant),  $v_{0y} = v_0 \sin \theta$  (then free-falls).

**Step 2 — fly** (level ground, up positive):

- Time to top:  $t = v_{0y}/g$  · Total flight:  $T = 2v_{0y}/g$
- Max height:  $H = v_{0y}^2/(2g)$  — units:  $(m/s)^2/(m/s^2) = m$  ✓
- Range:  $R = v_{0x} \cdot T$

At the top:  $v_y = 0$  but  $v_x$  is still going — the projectile is never at rest.

## WE DO Exercise 1: The Full Flight

A soccer ball is kicked at 20 m/s at 37° above horizontal from level ground. Find **(a)** the components, **(b)** the total flight time, **(c)** the maximum height, and **(d)** the range.

## YOUR TURN

### YOU DO Exercise 2: Steeper Kick

A ball is launched at 25 m/s at  $53^\circ$  above horizontal from level ground. Find the total flight time, maximum height, and range.

**Resolve once, at the start.** After Step 1, the launch speed  $v_0$  should never appear in your equations again — only  $v_{0x}$  and  $v_{0y}$ . Mixing  $v_0$  into a vertical equation is the #1 angled-launch error.

### YOU DO Exercise 3: Complementary Angles

Two identical balls are kicked at 20 m/s — one at  $30^\circ$ , one at  $60^\circ$ . For each, find the flight time and range. What do you notice about the ranges? Which ball wins on hang time?

## USE THE SYMMETRY

### SYMMETRY FACTS (LEVEL GROUND, NO AIR RESISTANCE)

- Time up = time down; the trajectory is a mirror image about the peak
- Landing speed = launch speed; landing angle = launch angle (below horizontal)
- Complementary launch angles ( $30^\circ/60^\circ$ ,  $37^\circ/53^\circ$ ) give equal ranges
- $45^\circ$  maximizes range — it splits  $v_0$  evenly between distance ( $v_x$ ) and airtime ( $v_y$ )

### CHALLENGE Exercise 4: No Calculator Needed

A ball launched at 26 m/s at  $40^\circ$  lands on level ground. **(a)** What is its landing speed? **(b)** What other launch angle at 26 m/s would land in the same spot? **(c)** Justify both answers in one sentence each — no computation allowed.

# PAPER PRACTICE

## PRACTICE PROBLEMS

### P1 Vertical Component

Find the initial vertical velocity component of a launch at 30 m/s at  $53^\circ$  above horizontal.

### P2 Hang Time

A projectile is launched with  $v_{oy} = 9.8$  m/s on level ground. How long is it airborne?

### P3 Full Analysis

A ball is launched at 19.6 m/s at  $30^\circ$  above horizontal on level ground. Find the flight time, maximum height, and range.

### P4 Best Angle

In one or two sentences: why does  $45^\circ$  give the maximum range on level ground? Frame your answer as a trade-off between the two components.