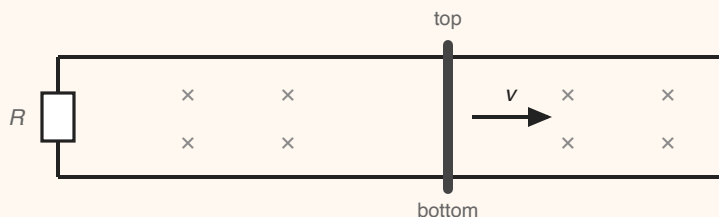


INDUCTION DAY 3: MOTIONAL EMF

WARMUP A Battery Made of Motion

Today's rig: a conducting bar slides RIGHT along two rails, through a field B pointing INTO the page. Every charge inside the bar rides along at v — so each feels $q\mathbf{v} \times \mathbf{B}$ directed along the bar. Which end of the bar — top or bottom — accumulates positive charge, and what has the bar become?



The bar-on-rails rig for the whole day. $\times = B$ into the page.

MOTIONAL EMF & THE ENERGY PIPELINE

$$\mathcal{E} = BLv \text{ (bar } \perp B, \text{ sliding } \perp \text{ its length)}$$

Close the circuit (resistance R) and the chain runs: $I = BLv/R \rightarrow$ the current-carrying bar feels $\mathbf{F} = \mathbf{BIL} = \mathbf{B^2 L^2 v/R}$ opposing the motion (Lenz) $\rightarrow$ keeping the bar moving costs $P = Fv = \mathcal{E}^2/R$, exactly the heat in R .
Faraday agrees: the enclosed area grows at rate Lv , so $d\Phi/dt = BLv$. Two derivations, one answer.

WE DO Exercise 1: The Full Chain

$B = 0.4 \text{ T}$, $L = 0.5 \text{ m}$, $v = 3.0 \text{ m/s}$, $R = 0.2 \Omega$. (a) $\mathcal{E} = BLv =$ _____. (b) $I =$ _____. (c) F on the bar = $BIL =$ _____. (d) $P = Fv =$ _____ = $\mathcal{E}^2/R =$ _____.

VARIATIONS ON THE BAR

WE DO Exercise 2: Terminal Velocity

The same rails tipped vertical: the bar ($m = 0.1 \text{ kg}$) falls, and the magnetic drag B^2L^2v/R grows with speed until it balances gravity. Set $B^2L^2v/R = mg$ and solve for the terminal speed ($B = 0.4 \text{ T}$, $L = 0.5 \text{ m}$, $R = 0.2 \Omega$, $g = 9.8 \text{ m/s}^2$).

YOU DO Exercise 3: Design the Bar

You need 1.5 V from a rail generator with $B = 0.5 \text{ T}$ and $v = 2.0 \text{ m/s}$. What bar length?

CALC Exercise 4: Faraday Route

Let $x(t)$ be the bar's position, so the enclosed area is $A = Lx$ and $\Phi = BLx$. Differentiate to show $\varepsilon = -d\Phi/dt$ has magnitude BLv — the flux derivation of the same law. State why the $qv \times B$ and $d\Phi/dt$ routes **MUST** agree.

PAPER PRACTICE

PRACTICE PROBLEMS

P1 BLv

$B = 0.5 \text{ T}$, $L = 0.8 \text{ m}$, $v = 4.0 \text{ m/s}$: find $\mathcal{E}$.

P2 Chain It

For P1 with $R = 0.4 \Omega$: find I and the drag force on the bar.

P3 Power Balance

For P1-P2, show $P = Fv$ and $P = \mathcal{E}^2/R$ give the same number.

P4 The Free-Wheeling Bar

The pushing hand lets go. Describe the bar's subsequent motion qualitatively — what force acts, how it depends on v , and what KIND of decay that produces (you know this shape from RC circuits).