

CIRCUITS DAY 3: SERIES & PARALLEL

WARMUP Opposite Day

Capacitors: parallel ADDED C , series added $1/C$. Resistors flip it. Before any formulas — why should MORE parallel paths mean LESS resistance? (Think doors out of a crowded room.)

COMBINING RESISTORS

Series (same I , voltages add): $R_{eq} = R_1 + R_2 + \dots$ — a longer pipe.

Parallel (same V , currents add): $1/R_{eq} = 1/R_1 + 1/R_2 + \dots$ — more doors. Two-resistor shortcut: product/sum. Always BELOW the smallest member.

The routine: collapse inside-out, Ohm the whole thing, then walk back out branch by branch.

WE DO Exercise 1: The Full Routine

A 24 V battery drives a $6.0\ \Omega$ resistor in series with a ($3.0\ \Omega \parallel 6.0\ \Omega$) pair. **(a)** $R_{\parallel} =$ _____. **(b)** $R_{total} =$ _____, $I_{battery} =$ _____. **(c)** V across the pair = _____. **(d)** Current in the $3.0\ \Omega$ branch = _____.

DIVIDERS AND CHECKS

WE DO Exercise 2: Voltage Divider

A $4.0\ \Omega$ and an $8.0\ \Omega$ resistor in series across 24 V . Same current everywhere — so the volts split in proportion to R : $V_4 = \underline{\hspace{2cm}}$, $V_8 = \underline{\hspace{2cm}}$ (check the sum).

YOU DO Exercise 3: Current Divider

A 12 V battery across a $4.0\ \Omega \parallel 12\ \Omega$ pair. Find the current in each branch and show the junction rule holds at the split.

CALC Exercise 4: Derive the Parallel Rule

Same V across both; currents add: $I = V/R_1 + V/R_2$. Divide by V to finish $1/R_{\text{eq}} = 1/R_1 + 1/R_2$. Then verify the "always smaller" claim: show $R_{\text{eq}} < R_1$ no matter what $R_2 > 0$ is.

PAPER PRACTICE

PRACTICE PROBLEMS

P1 Series

3.0 Ω , 5.0 Ω , and 4.0 Ω in series: R_{eq} ?

P2 Parallel

6.0 Ω and 12 Ω in parallel: R_{eq} ?

P3 Mixed Network

A 5.0 Ω resistor in series with (10 Ω || 10 Ω), across 20 V. Find R_{eq} and the battery current.

P4 Power Split

For P3's circuit, find the power dissipated in the series 5.0 Ω resistor and in EACH 10 Ω branch. Check that the three powers sum to the battery's output $P = IV$.