

CAPACITORS DAY 5: SERIES & PARALLEL

WARMUP Why the Same Q?

Two capacitors in series: the wire between them is an ISLAND — no charge can enter or leave it. If the left plate of the island pair holds $-Q$, what must the right plate hold, and why does that force both capacitors to carry identical Q ?

COMBINING CAPACITORS

Parallel (same ΔV , charges add): $C_{eq} = C_1 + C_2 + \dots$ — side-by-side plates are one BIGGER plate.

Series (same Q , voltages add): $1/C_{eq} = 1/C_1 + 1/C_2 + \dots$ — stacked gaps are one WIDER gap. Two-cap shortcut: $C_{eq} = C_1 C_2 / (C_1 + C_2)$.

Opposite of resistors-to-come. Series ALWAYS gives less than the smallest member.

WE DO Exercise 1: Both Ways

$C_1 = 2.0 \mu\text{F}$ and $C_2 = 3.0 \mu\text{F}$. **(a)** In parallel: $C_{eq} = \underline{\hspace{2cm}} \mu\text{F}$. **(b)** In series: $C_{eq} = (2 \cdot 3) / (2 + 3) = \underline{\hspace{2cm}} \mu\text{F}$.

DIVIDING THE VOLTS, DIVIDING THE CHARGE

WE DO Exercise 2: Series Division

The series pair ($C_{eq} = 1.2 \mu F$) goes across 10 V. **(a)** $Q = C_{eq} \cdot V = \underline{\hspace{2cm}} \mu C$ — on EACH capacitor. **(b)** $V_1 = Q/C_1 = \underline{\hspace{2cm}} V$, $V_2 = Q/C_2 = \underline{\hspace{2cm}} V$. **(c)** Check: they sum to $\underline{\hspace{2cm}}$.

YOU DO Exercise 3: Mixed Network

Two $2.0 \mu F$ capacitors in series, and that pair in parallel with a $3.0 \mu F$ capacitor. Find C_{eq} of the whole network.

CALC Exercise 4: Derive the Series Rule

Same Q on both; voltages add: $V = Q/C_1 + Q/C_2$. Divide by Q and finish the derivation of $1/C_{eq}$. Then explain geometrically: for two IDENTICAL plate capacitors stacked, what single capacitor is the stack equivalent to?

PAPER PRACTICE

PRACTICE PROBLEMS

P1 Parallel

2.0 μF , 3.0 μF , and 6.0 μF in parallel: C_{eq} ?

P2 Series

Three 6.0 μF capacitors in series: C_{eq} ?

P3 Network + Charge

A 6.0 μF in series with a 3.0 μF ; that pair in parallel with a 4.0 μF ; the network across 12 V. Find C_{eq} , then the total charge drawn from the battery.

P4 Series vs Parallel Energy

Two 4.0 μF capacitors across 12 V — once in series, once in parallel. Compute the total stored energy each way, and the ratio parallel/series.